**Theorem 1 (Residue Theorem).** Let f be analytic in the region G except for the isolated singularities  $a_1, a_2, \ldots, a_m$ . If  $\gamma$  is a closed rectifiable curve in G which does not pass through any of the points  $a_k$  and if  $\gamma \approx 0$  in G then

$$\frac{1}{2\pi i} \int_{\gamma} f = \sum_{k=1}^{m} n(\gamma; a_k) \operatorname{Res}(f; a_k).$$

**Theorem 2 (Maximum Modulus).** Let G be a bounded open set in  $\mathbb{C}$  and suppose that f is a continuous function on  $G^-$  which is analytic in G. Then

$$\max\{|f(z)| : z \in G^{-}\} = \max\{|f(z)| : z \in \partial G\}.$$